

Generally useful constants (MKS):

amu = 1.6605 (10⁻²⁷) kg
NA = 6.02221 (10²³) /mole
k = 1.38066 (10⁻²³) J / K
me = 9.1094 (10⁻³¹) kg
h = 6.62608 (10⁻³⁴) J s
q = 1.6022 (10⁻¹⁹) C
c = 2.9979 (10⁸) m / s

$$1.6605 \times 10^{-27} \text{ kg}$$

$$\frac{6.02221 \times 10^{23}}{\text{mole}}$$

$$\frac{1.38066 \times 10^{-23} \text{ J}}{\text{K}}$$

$$9.1094 \times 10^{-31} \text{ kg}$$

$$6.62608 \times 10^{-34} \text{ J s}$$

$$1.6022 \times 10^{-19} \text{ C}$$

$$\frac{2.9979 \times 10^8 \text{ m}}{\text{s}}$$

Problem 1.10 (Engel)

What speed does a H₂ molecule have if it has the same momentum as a photon of wavelength 280 nm?

Solution

Strategy. The problem says to equate the momenta of the molecule and the photon. First, calculate this momentum for the photon

$$p = \frac{h}{\lambda}$$

Next, convert this momentum to a velocity for the molecule

$$v = \frac{p}{m}$$

Execution. Calculate momenta for $\lambda = 280 \text{ nm}$ (but first convert nm to m).

$$\lambda = (280. \text{ nm}) \left(\frac{\text{m}}{10^9 \text{ nm}} \right)$$

$$2.8 \times 10^{-7} \text{ m}$$

$$p = h / \lambda$$

$$\frac{2.36646 \times 10^{-27} \text{ J s}}{\text{m}}$$

Calculate molecular mass of H_2

$$\text{mass} = 2 * 1.0079 \text{ amu}$$

$$3.34724 \times 10^{-27} \text{ kg}$$

Calculate velocity

$$v = p / \text{mass}$$

$$\frac{0.706988 \text{ J s}}{\text{kg m}}$$

My units look terribly complicated. Simplify by recognizing that $\text{J} = \text{kg m}^2 \text{ s}^{-2}$

$$v * \frac{\text{kg} * \text{m}^2}{\text{J} * \text{s}^2}$$

$$\frac{0.706988 \text{ m}}{\text{s}}$$

Comment

Can light slow down matter? It would seem so - all you have to do is direct a photon at an approaching molecule. But don't expect too much from *one* photon. H_2 is a *lightweight* molecule and 280 nm is a high-energy (near UV) photon. To slow down heavier molecules, one would need to use multiple photons (or maybe photons of even higher energy and momentum).